

# The Statistical Sleuth in R:

## Chapter 3

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## 1 Introduction

This document is intended to help describe how to undertake analyses introduced as examples in the Second Edition of the *Statistical Sleuth* (2002) by Fred Ramsey and Dan Schafer. More information about the book can be found at <http://www.proaxis.com/~panorama/home.htm>. This file as well as the associated `knitr` reproducible analysis source file can be found at <http://www.amherst.edu/~nhorton/sleuth>.

This work leverages initiatives undertaken by Project MOSAIC (<http://www.mosaic-web.org>), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the `mosaic` package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the `mosaic` package vignette (<http://cran.r-project.org/web/packages/mosaic/vignettes/MinimalR.pdf>).

To use a package within R, it must be installed (one time), and loaded (each session). The package can be installed using the following command:

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```
> install.packages('mosaic') # note the quotation marks
```

Once this is installed, it can be loaded by running the command:

```
> require(mosaic)
```

This needs to be done once per session.

In addition the data files for the *Sleuth* case studies can be accessed by installing the **Sleuth2** package.

```
> install.packages('Sleuth2') # note the quotation marks
```

```
> require(Sleuth2)
```

We also set some options to improve legibility of graphs and output.

```
> trellis.par.set(theme=col.mosaic()) # get a better color scheme for lattice
> options(digits=3, show.signif.stars=FALSE)
```

The specific goal of this document is to demonstrate how to calculate the quantities described in *Sleuth* Chapter 3: A Closer Look at Assumptions using R.

## 2 Cloud Seeding to Increase Rainfall

Does seeding clouds lead to more rainfall? This is the question being addressed by case study 3.1 in the *Sleuth*.

### 2.1 Summary statistics and graphical displays (untransformed)

We begin by reading the data and summarizing the variables.

```
> summary(case0301)
```

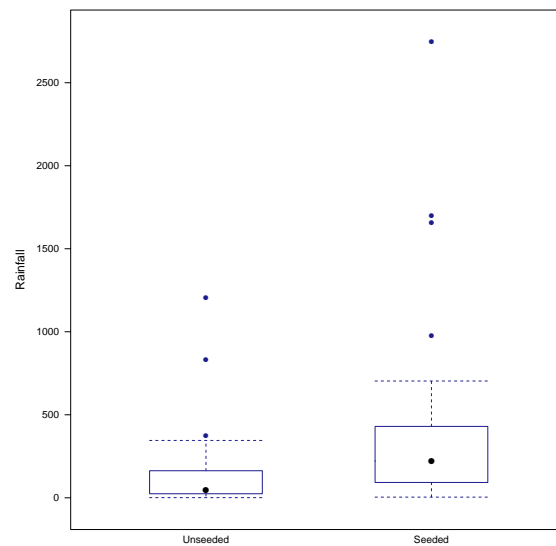
	Rainfall	Treatment
Min. :	1	Unseeded:26
1st Qu.:	29	Seeded :26
Median :	117	
Mean :	303	
3rd Qu.:	307	
Max. :	2746	

```
> favstats(Rainfall ~ Treatment, data=case0301)
```

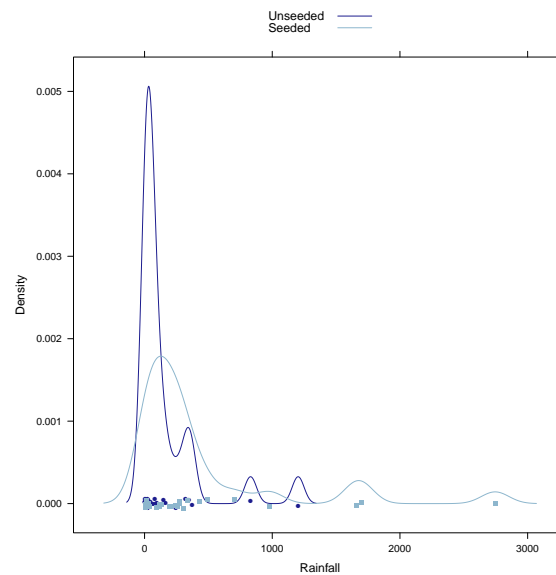
	Treatment	min	Q1	median	Q3	max	mean	sd	n	missing
1	Unseeded	1.0	24.8	44.2	159	1203	165	278	26	0
2	Seeded	4.1	98.1	221.6	406	2746	442	651	26	0

A total of 52 subjects were included in this data: 26 seeded days and 26 unseeded days (Display 3.1, page 57).

```
> bwplot(Rainfall ~ Treatment, data=case0301)
```



```
> densityplot(~Rainfall, groups=Treatment, auto.key=TRUE, data=case0301)
```



According to the boxplot and the density plot, the rainfall from seeded days seems to be larger than unseeded days. Both density curves are highly skewed to the right.

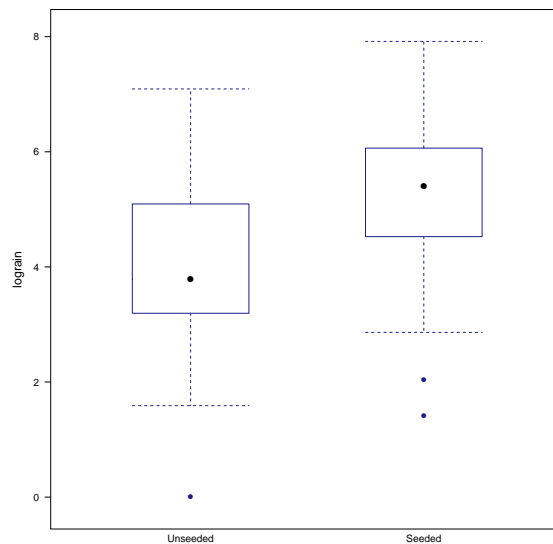
## 2.2 Summary statistics and graphical display (transformed)

The skewness suggests there is a need to apply the logarithmic transformation. The transformed data is shown on page 71 (Display 3.9).

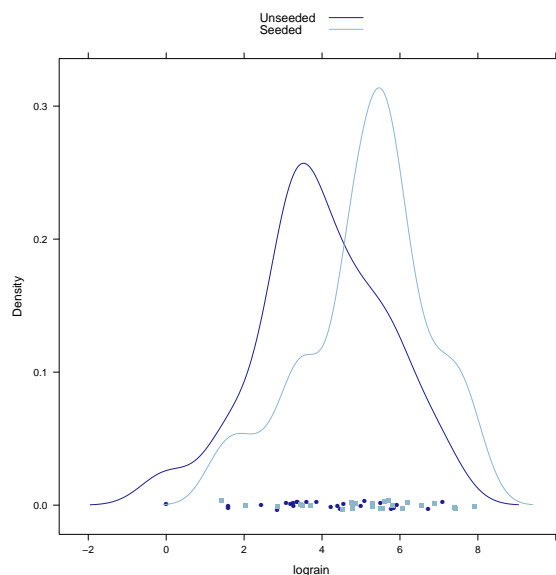
```
> case0301 = transform(case0301, lograin=log(Rainfall))
> favstats(lograin ~ Treatment, data=case0301)
```

Treatment	min	Q1	median	Q3	max	mean	sd	n	missing
1 Unseeded	0.00	3.21	3.79	5.07	7.09	3.99	1.64	26	0
2 Seeded	1.41	4.58	5.40	6.00	7.92	5.13	1.60	26	0

```
> bwplot(lograin ~ Treatment, data=case0301)
```



```
> densityplot(~lograin, groups=Treatment, auto.key=TRUE, data=case0301)
```



The log transformation reduces skewness of these two distributions.

### 2.3 Inferential procedures (two-sample t-test)

```
> t.test(Rainfall ~ Treatment, var.equal=FALSE, data=case0301)
```

Welch Two Sample t-test

```
data: Rainfall by Treatment
t = -2, df = 30, p-value = 0.05
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -559.56    4.76
sample estimates:
mean in group Unseeded   mean in group Seeded
                165                442
```

```
> t.test(Rainfall ~ Treatment, var.equal=TRUE, data=case0301)
```

Two Sample t-test

```
data: Rainfall by Treatment
t = -2, df = 50, p-value = 0.05
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -556.22    1.43
sample estimates:
```

mean in group Unseeded	mean in group Seeded
165	442

The following corresponds to the calculations on page 71.

```
> summary(lm(lograin ~ Treatment, data=case0301))

Call:
lm(formula = lograin ~ Treatment, data = case0301)

Residuals:
    Min       1Q   Median       3Q      Max
-3.990 -0.745  0.162  1.019  3.102

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)    3.990     0.318   12.55  <2e-16
TreatmentSeeded  1.144     0.450    2.54   0.014

Residual standard error: 1.62 on 50 degrees of freedom
Multiple R-squared:  0.115, Adjusted R-squared:  0.0969
F-statistic: 6.47 on 1 and 50 DF,  p-value: 0.0141

> ttestlog = t.test(lograin ~ Treatment, data=case0301); ttestlog

Welch Two Sample t-test

data:  lograin by Treatment
t = -3, df = 50, p-value = 0.01
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -2.047 -0.241
sample estimates:
mean in group Unseeded  mean in group Seeded
                3.99                5.13
```

The two-sided  $p$ -value is  $p = 0.014$  and the 95% confidence interval is between -2.05 and -0.24.

## 2.4 Interpretation of log model

The following code is used to calculate the “Summary of Statistical Findings” on page 57. First, we want to calculate the multiplier.

```
> obslogdiff = -diff(mean(lograin ~ Treatment, data=case0301)); obslogdiff

Seeded
-1.14

> multiplier = exp(obslogdiff); multiplier

Seeded
0.319
```

Next we can calculate the 95% confidence interval for the multiplier.

```
> tttestlog$conf.int

[1] -2.047 -0.241
attr("conf.level")
[1] 0.95

> exp(tttestlog$conf.int)

[1] 0.129 0.786
attr("conf.level")
[1] 0.95
```

### 3 Effects of Agent Orange on Troops in Vietnam

Is dioxin concentration related to veteran status? This is the question being addressed by case study 3.2 in the *Sleuth*.

#### 3.1 Summary statistics and graphical display

We begin by reading the data and summarizing the variables.

```
> summary(case0302)

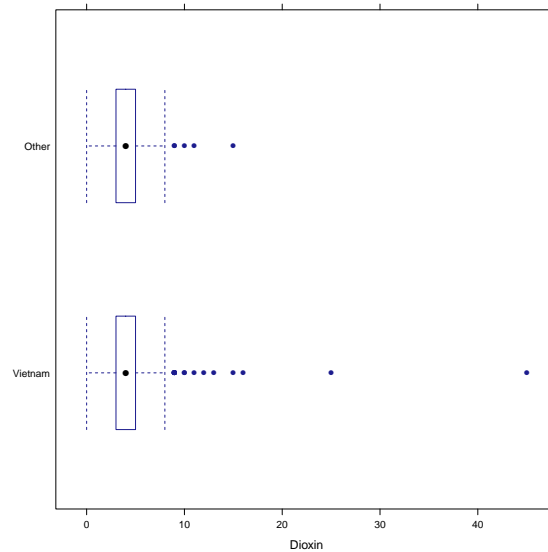
      Dioxin      Veteran
Min.   : 0.0   Vietnam:646
1st Qu.: 3.0   Other  : 97
Median : 4.0
Mean   : 4.3
3rd Qu.: 5.0
Max.   :45.0

> favstats(Dioxin ~ Veteran, data=case0302)

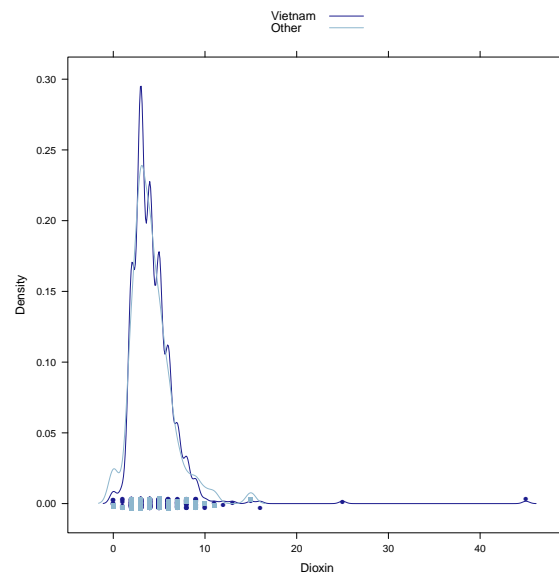
  Veteran min Q1 median Q3 max mean  sd  n missing
1 Vietnam  0  3     4  5  45 4.26 2.64 646      0
2  Other   0  3     4  5  15 4.19 2.30  97      0
```

A total of 743 veterans were included in this data: 646 served in Vietnam during 1967 and 1968 and 97 served in US or Germany during 1965 and 1971.

```
> bwplot(Veteran ~ Dioxin, data=case0302)
```



```
> densityplot(~Dioxin, groups=Veteran, auto.key=TRUE, data=case0302)
```



Both distributions are highly skewed to the right.

### 3.2 Inferential procedures (two-sample t-test)

The following code is used to calculate the “Summary of Statistical Findings” on page 60.



```

> t.test(Dioxin ~ Veteran, var.equal=TRUE, alternative="less", data=case0302)

Two Sample t-test

data: Dioxin by Veteran
t = 0.3, df = 700, p-value = 0.6
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
 -Inf 0.541
sample estimates:
mean in group Vietnam    mean in group Other
                4.26                4.19

> t.test(Dioxin ~ Veteran, var.equal=TRUE, data=case0302)$conf.int

[1] -0.482  0.631
attr(,"conf.level")
[1] 0.95

```

So the one-sided  $p$ -value from a two-sample  $t$ -test is 0.604. The 95% confidence interval is (-0.48, 0.63).

### 3.3 Removing outliers

We will remove two extreme observations from the data. First we remove observation 646 and perform a  $t$ -test (Display 3.7, page 67).

```

> case0302.2 = case0302[-c(646), ]
> t.test(Dioxin ~ Veteran, alternative="less", data=case0302.2)

Welch Two Sample t-test

data: Dioxin by Veteran
t = 0.05, df = 100, p-value = 0.5
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
 -Inf 0.422
sample estimates:
mean in group Vietnam    mean in group Other
                4.20                4.19

```

Next we remove observations 645 and 646 and perform a  $t$ -test.

```
> dim(case0302)

[1] 743  2

> case0302.3 = case0302[-c(645, 646), ]
> dim(case0302.3)

[1] 741  2

> t.test(Dioxin ~ Veteran, alternative="less", data=case0302.3)

Welch Two Sample t-test

data: Dioxin by Veteran
t = -0.09, df = 100, p-value = 0.5
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
 -Inf 0.387
sample estimates:
mean in group Vietnam    mean in group Other
                4.16                4.19
```

Notice that after removing these outliers, the  $p$ -value and the confidence interval have changed but the substantive conclusion is unchanged.